

Binomische Formeln (Level 2)

Aufgabe

Multipliziere die folgenden Terme mit Hilfe der binomischen Formeln aus:

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|--------------------------------|--------------------------------|--------------------------------|
| a) $(7p + 8x) \cdot (7p - 8x)$ | b) $(2q + 2w)^2$ | c) $(4n + v)^2$ |
| d) $(10k - 9z)^2$ | e) $(4m - 2e)^2$ | f) $(8a + 9t)^2$ |
| g) $(10s + 7q)^2$ | h) $(10t - 6d)^2$ | i) $(8s + 8x) \cdot (8s - 8x)$ |
| j) $(3d - 3w)^2$ | k) $(5w + 5b)^2$ | l) $(3y + 3r)^2$ |
| m) $(5t - 2m)^2$ | n) $(2r + 2u)^2$ | o) $(7r - 10r)^2$ |
| p) $(8m - 2y)^2$ | q) $(p + 3u) \cdot (p - 3u)$ | r) $(3k - 7m)^2$ |
| s) $(5k + 4c)^2$ | t) $(10z - 8c)^2$ | u) $(5a + 2p) \cdot (5a - 2p)$ |
| v) $(7p + 7t)^2$ | w) $(4e + 5w) \cdot (4e - 5w)$ | x) $(d + 4t)^2$ |
| y) $(7c - 9v)^2$ | z) $(8e + 9d) \cdot (8e - 9d)$ | |

Tipp

Es gibt drei binomische Formeln:

- I. $(a + b)^2 = a^2 + 2ab + b^2$
- II. $(a - b)^2 = a^2 - 2ab + b^2$
- III. $(a + b) \cdot (a - b) = a^2 - b^2$

Rechenweg

- a) $(7p + 8x) \cdot (7p - 8x) = (7p)^2 - (8x)^2 = 49p^2 - 64x^2$
- b) $(2q + 2w)^2 = (2q)^2 + 2 \cdot 2q \cdot 2w + (2w)^2 = 4q^2 + 8qw + 4w^2$
- c) $(4n + v)^2 = (4n)^2 + 2 \cdot 4n \cdot v + v^2 = 16n^2 + 8nv + v^2$
- d) $(10k - 9z)^2 = (10k)^2 - 2 \cdot 10k \cdot 9z + (9z)^2 = 100k^2 - 180kz + 81z^2$
- e) $(4m - 2e)^2 = (4m)^2 - 2 \cdot 4m \cdot 2e + (2e)^2 = 16m^2 - 16em + 4e^2$
- f) $(8a + 9t)^2 = (8a)^2 + 2 \cdot 8a \cdot 9t + (9t)^2 = 64a^2 + 144at + 81t^2$
- g) $(10s + 7q)^2 = (10s)^2 + 2 \cdot 10s \cdot 7q + (7q)^2 = 100s^2 + 140qs + 49q^2$
- h) $(10t - 6d)^2 = (10t)^2 - 2 \cdot 10t \cdot 6d + (6d)^2 = 100t^2 - 120dt + 36d^2$
- i) $(8s + 8x) \cdot (8s - 8x) = (8s)^2 - (8x)^2 = 64s^2 - 64x^2$
- j) $(3d - 3w)^2 = (3d)^2 - 2 \cdot 3d \cdot 3w + (3w)^2 = 9d^2 - 18dw + 9w^2$
- k) $(5w + 5b)^2 = (5w)^2 + 2 \cdot 5w \cdot 5b + (5b)^2 = 25w^2 + 50bw + 25b^2$
- l) $(3y + 3r)^2 = (3y)^2 + 2 \cdot 3y \cdot 3r + (3r)^2 = 9y^2 + 18ry + 9r^2$
- m) $(5t - 2m)^2 = (5t)^2 - 2 \cdot 5t \cdot 2m + (2m)^2 = 25t^2 - 20mt + 4m^2$
- n) $(2r + 2u)^2 = (2r)^2 + 2 \cdot 2r \cdot 2u + (2u)^2 = 4r^2 + 8ru + 4u^2$
- o) $(7r - 10r)^2 = (7r)^2 - 2 \cdot 7r \cdot 10r + (10r)^2 = 49r^2 - 140r^2 + 100r^2$
- p) $(8m - 2y)^2 = (8m)^2 - 2 \cdot 8m \cdot 2y + (2y)^2 = 64m^2 - 32my + 4y^2$
- q) $(p + 3u) \cdot (p - 3u) = p^2 - (3u)^2 = p^2 - 9u^2$
- r) $(3k - 7m)^2 = (3k)^2 - 2 \cdot 3k \cdot 7m + (7m)^2 = 9k^2 - 42km + 49m^2$
- s) $(5k + 4c)^2 = (5k)^2 + 2 \cdot 5k \cdot 4c + (4c)^2 = 25k^2 + 40ck + 16c^2$
- t) $(10z - 8c)^2 = (10z)^2 - 2 \cdot 10z \cdot 8c + (8c)^2 = 100z^2 - 160cz + 64c^2$
- u) $(5a + 2p) \cdot (5a - 2p) = (5a)^2 - (2p)^2 = 25a^2 - 4p^2$
- v) $(7p + 7t)^2 = (7p)^2 + 2 \cdot 7p \cdot 7t + (7t)^2 = 49p^2 + 98pt + 49t^2$
- w) $(4e + 5w) \cdot (4e - 5w) = (4e)^2 - (5w)^2 = 16e^2 - 25w^2$
- x) $(d + 4t)^2 = d^2 + 2 \cdot d \cdot 4t + (4t)^2 = d^2 + 8dt + 16t^2$

$$y) \quad (\textcolor{blue}{7} \, c - \textcolor{red}{9} \, v)^2 = (\textcolor{blue}{7} \, c)^2 - 2 \cdot \textcolor{blue}{7} \, c \cdot \textcolor{red}{9} \, v + (\textcolor{red}{9} \, v)^2 = 49 \, c^2 - 126 \, c \, v + 81 \, v^2$$

$$z) \quad (\textcolor{blue}{8} \, e + \textcolor{red}{9} \, d) \cdot (\textcolor{blue}{8} \, e - \textcolor{red}{9} \, d) = (\textcolor{blue}{8} \, e)^2 - (\textcolor{red}{9} \, d)^2 = 64 \, e^2 - 81 \, d^2$$

Lösung

a) $49 p^2 - 64 x^2$

d) $100 k^2 - 180 k z + 81 z^2$

g) $100 s^2 + 140 q s + 49 q^2$

j) $9 d^2 - 18 d w + 9 w^2$

m) $25 t^2 - 20 m t + 4 m^2$

p) $64 m^2 - 32 m y + 4 y^2$

s) $25 k^2 + 40 c k + 16 c^2$

v) $49 p^2 + 98 p t + 49 t^2$

y) $49 c^2 - 126 c v + 81 v^2$

b) $4 q^2 + 8 q w + 4 w^2$

e) $16 m^2 - 16 e m + 4 e^2$

h) $100 t^2 - 120 d t + 36 d^2$

k) $25 w^2 + 50 b w + 25 b^2$

n) $4 r^2 + 8 r u + 4 u^2$

q) $p^2 - 9 u^2$

t) $100 z^2 - 160 c z + 64 c^2$

w) $16 e^2 - 25 w^2$

z) $64 e^2 - 81 d^2$

c) $16 n^2 + 8 n v + v^2$

f) $64 a^2 + 144 a t + 81 t^2$

i) $64 s^2 - 64 x^2$

l) $9 y^2 + 18 r y + 9 r^2$

o) $49 r^2 - 140 r^2 + 100 r^2$

r) $9 k^2 - 42 k m + 49 m^2$

u) $25 a^2 - 4 p^2$

x) $d^2 + 8 d t + 16 t^2$